

## Electromagnetic Induction

*Motional emf:*  $\varepsilon = vBL$  if  $\vec{v}$ ,  $\vec{B}$ , and  $L$  are  $\perp$

**Magnetic flux:**

$$\Phi_B = BA \cos \theta \quad \theta \text{ is the angle between } \vec{B} \text{ and } \vec{A}$$

The magnetic flux changes if:

- the magnetic field  $\vec{B}$  changes
- the area of the coil within  $\vec{B}$  changes
- the angle between  $\vec{B}$  and  $\vec{A}$  changes

$\Rightarrow$  the current induced in a coil arises from an induced electromotive force or emf

**Faraday's law:**

$$\varepsilon = -N \frac{\Delta \Phi}{\Delta t} \quad * \text{ - sign indicates that induced emf opposes the change in magnetic flux}$$

$\Rightarrow$  the induced current is given by:  $i = \frac{\varepsilon}{R}$

**Lenz's law:**

*Lenz's law:* an induced current has a direction such that the magnetic field due to the current opposes the change in the magnetic flux that induces the current

\* if  $\Phi$  is decreasing, the induced current produces a  $\vec{B}$  field in the same direction as the original field (the induced magnetic field reinforces the original field)

\* if  $\Phi$  is increasing, the induced current produces a  $\vec{B}$  field in the opposite direction as the original field (the induced magnetic field opposes the original field)

**Transformers:**

$$\frac{\varepsilon_2}{\varepsilon_1} = \frac{N_2}{N_1}$$

$$\frac{I_2}{I_1} = \frac{\varepsilon_1}{\varepsilon_2} = \frac{N_1}{N_2}$$