

$$\text{ave.} = 5.1$$

$$\sigma = 2.4$$

Name Answer Key

Lab: early late (please circle one)

Quiz #7: Using Energy and Thermal Properties of Matter

Problem 1 (2 points)

Helium gas at 20 °C is confined within a rigid vessel. The gas is then heated until its pressure is doubled. What is the final temperature of the gas?

- a) 10 °C
b) 20 °C
c) 40 °C
d) 313 °C
e) 586 °C

$$pV = nRT \rightarrow T = \frac{pV}{nR}$$

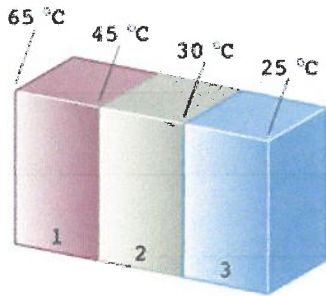
for constant n & V , doubling p doubles T , but T must be in Kelvin

$$T_i = 293K$$

$$T_f = 2(293K) = 586K = \boxed{313^\circ C}$$

Problem 2 (2 points)

The drawing shows a composite slab consisting of three materials through which heat is conducted from left to right at a constant rate. The materials have identical thicknesses and cross-sectional areas.



$$\frac{Q}{\Delta t} = \frac{KA\Delta T}{L} \rightarrow K = \frac{(Q/\Delta t)L}{A\Delta T} \rightarrow K \propto \frac{1}{\Delta T}$$

Which material (1, 2, or 3) has the largest thermal conductivity?

material 3 → the better a conductor, the smaller ΔT

Which material (1, 2, or 3) has the smallest thermal conductivity?

material 1 → the worse a conductor, the greater ΔT

Problem 3 (2 points)

Walking at a brisk pace uses energy at a rate of about 380 W. How many Calories would the human body burn while walking for 45 minutes? Take into account the efficiency of the human body.

$$P = E/t = 380W$$

$$E = Pt = (380W)(2700s)$$

$$t = 45 \text{ min} = 2700s$$

$$= \underline{1.026 \times 10^6 J}$$

$$1 \text{ Cal} = 4186 J$$

$$E = 1.026 \times 10^6 J \left(\frac{1 \text{ Cal}}{4186 J} \right) = \boxed{245 \text{ Cal}}$$

note: the rate 380W is rate at which we are "burning energy" and takes into account the efficiency of the human body (0.25). For every 4 Calories burned, we only get 1 Cal of useful output energy.

Problem 4 (4 points)

A 125.0-kg block of ice has a temperature of $-10.0\text{ }^{\circ}\text{C}$. The block of ice then absorbs $6.20 \times 10^7\text{ J}$ of heat. What is the final phase (solid, liquid or gas) and temperature?

$$c_{\text{water}} = 4186\text{ J/(kg }^{\circ}\text{C}^{\circ})$$

$$c_{\text{ice}} = 2.00 \times 10^3\text{ J/(kg }^{\circ}\text{C}^{\circ})$$

$$L_f = 3.33 \times 10^5\text{ J/kg}$$

$$L_v = 22.6 \times 10^5\text{ J/kg}$$

changing temp of ice
from $-10.0\text{ }^{\circ}\text{C} \rightarrow 0\text{ }^{\circ}\text{C}$ requires

$$Q = M_{\text{ice}} c_{\text{ice}} \Delta T_{\text{ice}}$$

$$Q = (125.0\text{ kg})(2.00 \times 10^3\text{ J/kg}\cdot^{\circ}\text{C})(10.0\text{ }^{\circ}\text{C}) = \underline{\underline{2.50 \times 10^6\text{ J}}}$$

melting ice requires

$$Q = M L_f = (125.0\text{ kg})(3.33 \times 10^5\text{ J/kg}) \\ = \underline{\underline{4.16 \times 10^7\text{ J}}}$$

changing temp. of water
from $0\text{ }^{\circ}\text{C}$ to $100\text{ }^{\circ}\text{C}$ requires

$$Q = (125.0\text{ kg})(4186\text{ J/kg}\cdot^{\circ}\text{C})(100.0\text{ }^{\circ}\text{C}) = \underline{\underline{5.23 \times 10^7\text{ J}}}$$

\Rightarrow there is not enough energy to change temp of water to $100\text{ }^{\circ}\text{C}$.

Energy left to change temp. of water:

$$Q = 6.20 \times 10^7\text{ J} - 2.50 \times 10^6\text{ J} - 4.16 \times 10^7\text{ J} = \underline{\underline{1.79 \times 10^7\text{ J}}}$$

$$Q = M_{\text{water}} c_{\text{water}} \Delta T_{\text{water}} \rightarrow \Delta T_{\text{water}} = \frac{Q}{M_{\text{water}} c_{\text{water}}}$$

$$\Delta T = \frac{1.79 \times 10^7\text{ J}}{(125.0\text{ kg})(4186\text{ J/kg}\cdot^{\circ}\text{C})} = \underline{\underline{34.2\text{ }^{\circ}\text{C}}} \quad (\text{Ti of water after melting is } 0\text{ }^{\circ}\text{C})$$

\Rightarrow final phase is water at $34.2\text{ }^{\circ}\text{C}$