

$$\text{ave.} = 8.6$$

$$\sigma = 1.7$$

**Quiz #3: Vectors and Coordinate Systems**

**Problem 1 (2 points)**

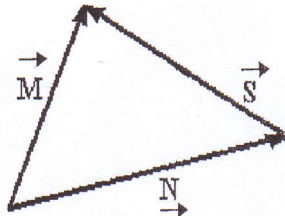
For the vectors shown in the figure, express vector  $\vec{S}$  in terms of vectors  $\vec{M}$  and  $\vec{N}$ .

a)  $\vec{S} = \vec{M} + \vec{N}$

b)  $\vec{S} = \vec{M} - \vec{N}$

c)  $\vec{S} = \vec{N} - \vec{M}$

d) none of the above



$$\vec{N} + \vec{S} = \vec{M}$$

$$\vec{S} = \vec{M} - \vec{N}$$

B

**Problem 2 (3 points)**

Vector  $\vec{A} = -2.00\hat{i} + 4.00\hat{j}$  and vector  $\vec{B} = 4.00\hat{i} - 3.00\hat{j}$ . What are the magnitude and direction of vector  $\vec{C} = 3.00\vec{A} + 2.00\vec{B}$ ?

$$C_x = 3A_x + 2B_x = 3(-2.00) + 2(4.00) = \underline{2.00}$$

$$\vec{C} = (2.00)\hat{i} + (6.00)\hat{j}$$

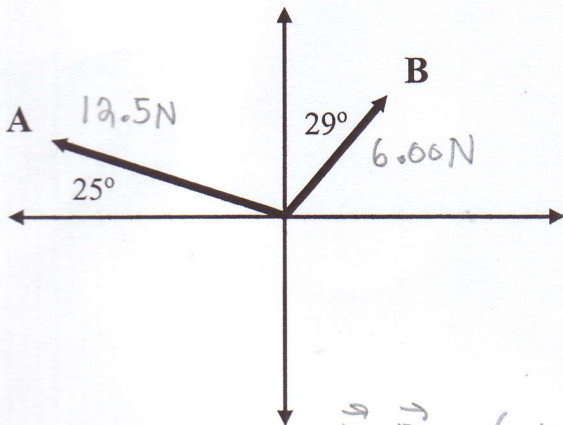
$$C_y = 3A_y + 2B_y = 3(4.00) + 2(-3.00) = \underline{6.00}$$

$$|\vec{C}| = \sqrt{(2.00)^2 + (6.00)^2} \rightarrow \underline{|\vec{C}| = 6.32}$$

$$\theta = \tan^{-1}\left(\frac{6.00}{2.00}\right) \rightarrow \underline{\theta = 71.6^\circ}$$

**Problem 3 (5 points)**

Two force vectors,  $\vec{A}$  and  $\vec{B}$ , are shown below. Force  $\vec{A}$  has a magnitude of 12.5 N and force  $\vec{B}$  has a magnitude of 6.00 N. Find the magnitude and direction of  $\vec{A} - \vec{B}$ .



$$\begin{aligned} \vec{A} &= -(12.5\text{N})\cos 25^\circ \hat{i} + (12.5\text{N})\sin 25^\circ \hat{j} \\ &= \underline{(-11.3\text{N})} \hat{i} + \underline{(5.28\text{N})} \hat{j} \end{aligned}$$

$$\begin{aligned} \vec{B} &= (6.00\text{N})\sin 29^\circ \hat{i} + (6.00\text{N})\cos 29^\circ \hat{j} \\ &= \underline{(2.91\text{N})} \hat{i} + \underline{(5.25\text{N})} \hat{j} \end{aligned}$$

$$\begin{aligned} \vec{A} - \vec{B} &= (-11.3\text{N} - 2.91\text{N})\hat{i} + (5.28\text{N} - 5.25\text{N})\hat{j} \\ &= \underline{(-14.2\text{N})} \hat{i} + \underline{(0.03\text{N})} \hat{j} \end{aligned}$$

$$|\vec{A} - \vec{B}| = \sqrt{(-14.2\text{N})^2 + (0.03\text{N})^2} = \underline{14.2\text{N}}$$

$$\theta = \tan^{-1}\left(\frac{0.03\text{N}}{-14.2\text{N}}\right) = -0.12^\circ \rightarrow \text{wrong quadrant} \rightarrow \underline{\theta = 180^\circ}$$