

Quiz #9: Impulse and Momentum

Problem 1 (2 points)

A rifle of mass M is initially at rest but free to recoil. It fires a bullet of mass m and velocity v (relative to the ground). After firing, the velocity of the rifle (relative to the ground) is:

- a) $-mv$
- b) $-Mv/m$
- c) $-mv/M$
- d) $-v$
- e) mv/M

$$\vec{P}_i = \vec{P}_f$$

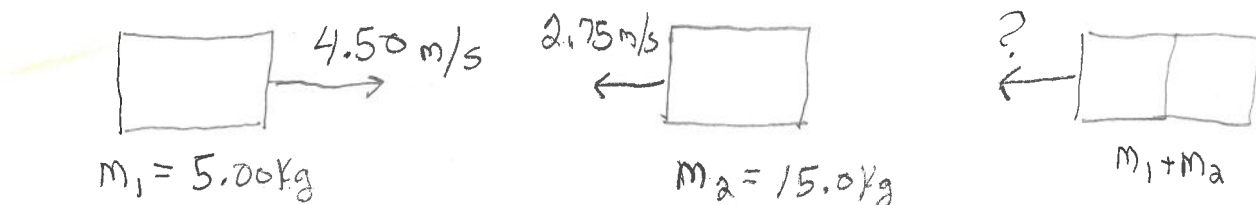
$$0 = mv + Mv_{\text{rifle}}$$

$$v_{\text{rifle}} = -\frac{mv}{M}$$

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Problem 2 (4 points)

A 5.00 kg object is traveling at 4.50 m/s to the right and collides with a 15.0 kg object traveling at 2.75 m/s to the left. If the two objects stick together after the collision, what is their combined velocity after the collision?



system \rightarrow both objects

$$\sum F_{\text{ext},x} = 0 \rightarrow P_{f,x} = P_{i,x}$$

$$(m_1 + m_2) v_{f,x} = m_1 v_{i1,x} + m_2 v_{i2,x}$$

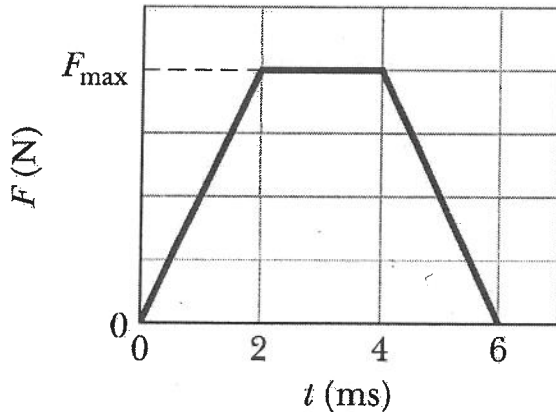
$$v_{f,x} = \frac{m_1 v_{i1,x} + m_2 v_{i2,x}}{(m_1 + m_2)}$$

$$v_{f,x} = \frac{(5.00\text{kg})(4.50\text{m/s}) + (15.0\text{kg})(-2.75\text{m/s})}{(5.00\text{kg} + 15.0\text{kg})}$$

$$v_{f,x} = -0.938 \text{ m/s}$$

Problem 3 (4 points)

The figure below shows the magnitude of the force F versus time t during the collision of a 75 g superball with a wall. The initial velocity of the ball is 32 m/s perpendicular to the wall. The ball rebounds directly back with a speed of 28 m/s, also perpendicular to the wall. What is F_{\max} , the maximum magnitude of the force on the ball from the wall during the collision? (Note: time is in milliseconds)



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$$\left. \begin{array}{l} \leftarrow \text{O} \quad v_{ix} = -32 \text{ m/s} \\ \text{O} \rightarrow \quad v_{fx} = +28 \text{ m/s} \end{array} \right\}$$

$$\Delta p_x = m (v_{fx} - v_{ix})$$

$$= (0.075 \text{ kg}) [28 \text{ m/s} - (-32 \text{ m/s})]$$

$$\Delta p_x = \underline{4.5 \text{ kg m/s}}$$

$$J_x = \text{area under curve of } F_x \text{ vs. } t = \Delta p_x$$

$$J_x = \frac{1}{2} F_{\max} (2 \text{ ms}) + F_{\max} (2 \text{ ms}) + \frac{1}{2} F_{\max} (2 \text{ ms}) = \Delta p_x$$

$$F_{\max} (4 \text{ ms}) = \Delta p_x \rightarrow F_{\max} = \frac{\Delta p_x}{(4 \text{ ms})}$$

$$F_{\max} = \frac{4.5 \text{ kg m/s}}{(4.0 \times 10^{-3} \text{ s})} \rightarrow \boxed{\begin{array}{l} F_{\max} = 1125 \text{ N} \\ = 1 \times 10^3 \text{ N} \end{array}}$$