

# LAB 5

## Capacitors

### OBJECTIVES

1. Study of the equivalent capacitance of capacitors connected in series and parallel.
2. Investigate the capacitance of the electrometer.

### EQUIPMENT

Capacitors (two each: 0.05  $\mu\text{F}$ , 0.10  $\mu\text{F}$ , and 0.22  $\mu\text{F}$ , and one 200 pF), electrometer, DC power supply, digital multimeter, breadboard.

### THEORY

Any arrangement that stores charge can properly be called a *capacitor*. The capacitance of a capacitor is a measure of how much charge can be stored on the capacitor for a given potential difference (voltage). The relation between charge  $q$ , voltage  $V$ , and capacitance  $C$  is given by:

$$q = CV \text{ or } C = \frac{q}{V}.$$

When two or more capacitors are connected together, they may be replaced by a single capacitor that has the same capacitance ( $C_{eq}$ ) as the combination of capacitors. For two capacitors connected in *parallel*, the equivalent capacitance is given by:

$$C_{eq} = C_1 + C_2.$$

For two capacitors connected in *series*, the equivalent capacitance is given by:

$$1/C_{eq} = 1/C_1 + 1/C_2.$$

If a capacitor  $C_1$  is connected to a power supply with voltage  $V_0$ , it will acquire a charge  $q$  given by  $q = C_1 V_0$ . If that capacitor is then disconnected from the power supply and connected in parallel to an initially uncharged capacitor  $C_2$ , the original charge  $q$  on capacitor 1 is split between the two capacitors. We therefore end up with the relation  $q = q_1 + q_2$ , where  $q_1$  and  $q_2$  are the final charges on capacitors 1 and 2. Since capacitors 1 and 2 are in parallel, they must have the same voltage  $V$ . The relationship  $q = q_1 + q_2$  therefore becomes  $C_1 V_0 = C_1 V + C_2 V$ .

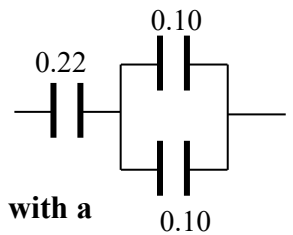
## PROCEDURE

### Part 1: Measuring the Unknown Capacitance $C_X$

- Measure the individual capacitance values (using a DMM) of the following two capacitors:  $0.05\ \mu\text{F}$  and  $0.10\ \mu\text{F}$ .
- Using the measured capacitance values, calculate the unknown capacitance  $(C_X)_{\text{thy}}$  by combining
  - $0.05\ \mu\text{F}$  in series with the  $C_X$
  - $0.10\ \mu\text{F}$  in series with the  $C_X$
  - $0.05\ \mu\text{F}$  and  $0.10\ \mu\text{F}$  in series with the  $C_X$
  - $0.05\ \mu\text{F}$  and  $0.10\ \mu\text{F}$  in parallel with  $C_X$Average these four values to obtain  $(C_X)_{\text{thy}}$ .
- Measure the unknown capacitance  $(C_X)_{\text{expt}}$  using the DMM and compare it with the averaged  $(C_X)_{\text{thy}}$  using a percent difference. *How do they compare?*

### Part 2: Charged Capacitor Connected in Parallel with Initially Uncharged Capacitors

- Set the output of the power supply to  $10\ \text{V}$  using the digital multimeter. After you have set the output voltage to  $10\ \text{V}$ , **do not** touch the voltage setting of the power supply for the rest of lab. Check the voltage of the power supply using the electrometer.
- Connect a  $0.05\ \mu\text{F}$  capacitor to two leads on the breadboard and then connect the electrometer to the ends of the capacitor. Keep the electrometer connected across the  $0.05\ \mu\text{F}$  capacitor for the entire lab.
- Charge the  $0.50\ \mu\text{F}$  capacitor by connecting it to the power supply. After the capacitor is fully charged (one or two seconds), disconnect the power supply. **Be careful not to touch either side of the capacitor or you will discharge it.**
- Predict what the voltage across the  $0.05\ \mu\text{F}$  capacitor will read after it is connected in parallel with the following six combinations of uncharged capacitors:*
  - one  $0.05\ \mu\text{F}$  capacitor**
  - one  $0.10\ \mu\text{F}$  capacitor**
  - two  $0.10\ \mu\text{F}$  capacitors in parallel**
  - two  $0.10\ \mu\text{F}$  capacitors in series**
  - a combination of two  $0.10\ \mu\text{F}$  capacitors in parallel in series with a third  $0.22\ \mu\text{F}$  capacitor**



- Connect the initially uncharged capacitor(s) in parallel with the charged  $0.05\ \mu\text{F}$  capacitor. Measure the voltage across the  $0.05\ \mu\text{F}$  capacitor with the electrometer and compare with your prediction. *Was your prediction correct? Report on your results.*
- Discharge all capacitors by touching both plates of each capacitor at the same time with a wire. Repeats steps (c) and (e) for all six combinations of uncharged capacitors.

### Part 3: Capacitance of the Electrometer

- Connect the  **$200\ \text{pF}$**  capacitor to the power supply. After the capacitor is fully charged (one or two seconds), disconnect the power supply.

- (b) Predict what the voltage across the 200 pF capacitor will be when you read the voltage using the electrometer.
- (c) Use the electrometer to measure the voltage across the 200 pF capacitor. *Was your prediction correct? Report on your results and any possible reasons for the discrepancy.*
- (d) *Use your results from part (c) to calculate the capacitance of the electrometer.*
- (e) *Why didn't the capacitance of the electrometer have a noticeable effect on the results from Part 2?*