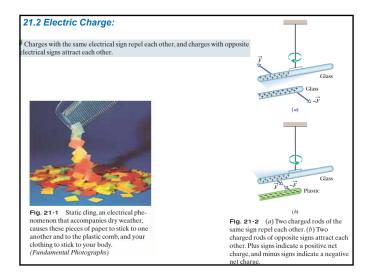
# Chapter 21

# **Electric Charge**



#### 21.3 Conductors and Insulators

Conductors are materials through which charge can move freely; examples include metals (such as copper in common lamp wire), the human body, and tap water.

Nonconductors—also called insulators—are materials through which charge cannot move freely; examples include *rubber*, *plastic*, *glass*, *and chemically pure water*.

**Semiconductors** are materials that are intermediate between conductors and insulators; examples include *silicon and germanium in computer chips*.

**Superconductors** are materials that are perfect conductors, allowing charge to move without any hindrance.

The properties of conductors and insulators are due to the structure and electrical nature of atoms.

Atoms consist of positively charged *protons*, negatively charged *electrons*, and electrically neutral *neutrons*. The protons and neutrons are packed tightly together in a central nucleus.

When atoms of a conductor come together to form the solid, some of their outermost (and so most loosely held) electrons become free to wander about within the solid, leaving behind positively charged atoms ( positive ions). We call the mobile electrons conduction electrons.

There are few (if any) free electrons in a nonconductor.

## 21.3 Conductors and Insulators

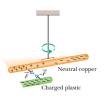




Fig. 21-5 Two pieces of a wintergreen LifeSaver candy as they fall away from each other. Electrons jumping from the negative surface of piece A to the positive surface of piece B collide with nitrogen  $(N_2)$  molecules in the air.

Fig. 21-4 A neutral copper rod is electrically isolated from its surroundings by being suspended on a nonconducting thread. Either end of the copper rod will be attracted by a charged rod. Here, conduction electrons in the copper rod are repelled to the far end of that rod by the negative charge on the plastic rod. Then that negative charge attracts the remaining positive charge on the near end of the copper rod, rotating the copper rod to bring that near end closer to the plastic rod.

#### 21.4 Coulomb's Law

This force of repulsion or attraction due to the charge properties of objects is called an **electrostatic force**.

The equation giving the force for charged particles is called **Coulomb's law:** 

$$\vec{F} = k \frac{q_1 q_2}{r^2} \hat{\mathbf{r}}$$
 (Coulomb's law),

where particle 1 has charge  $q_1$  and particle 2 has charge  $q_2$  and F is the force on particle 1. Here iis a unit vector along an axis extending through the two particles, r is the distance between them  $\frac{1}{7}$  nd K is a constant.

The SI unit of charge is the *coulomb*.

The constant  $k = \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \,\text{N} \cdot \text{m}^2/\text{C}^2$ .

The quantity  $\boldsymbol{\epsilon}_0$  is called the permittivity constant

$$\varepsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2.$$

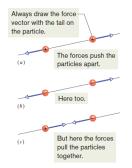


Fig. 21-6 Two charged particles repel each other if they have the same sign of charge, either (a) both positive or (b) both negative. (c) They attract each other if they have opposite signs of charge.

#### 21.4 Coulomb's Law

Current is the rate dq/dt at which charge moves past a point or through a region

$$i = \frac{dq}{dt}$$
 (electric current),

in which i is the current (in amperes) and dq (in coulombs) is the amount of charge moving past a point or through a region in time dt (in seconds).

Therefore,

1 C = (1 A)(1 s).

#### 21.4 Coulomb's Law

If there are n charged particles, they interact independently in pairs, and the force on any one of them, say particle 1, is given by the vector sum

$$\vec{F}_{1,\text{net}} = \vec{F}_{12} + \vec{F}_{13} + \vec{F}_{14} + \vec{F}_{15} + \dots + \vec{F}_{1n}$$

in which,  $\mathbf{F}_{1,4}$  is the force acting on particle 1 due to the presence of particle 4 etc

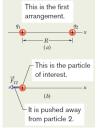
As with gravitational force law, the shell theorem has analogs in electrostatics:

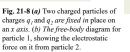
A shell of uniform charge attracts or repels a charged particle that is outside the shell as if all the shell's charge were concentrated at its center.

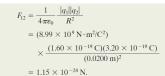
■ If a charged particle is located inside a shell of uniform charge, there is no net electrostatic force on the particle from the shell.

#### Example, The net force due to two other particles:

(a) Figure 21-8a shows two positively charged particles fixed in place on an x axis. The charges are  $q_1=1.60\times 10^{-19}$  C and  $q_2=3.20\times 10^{-19}$  C, and the particle separation is R=0.0200 m. What are the magnitude and direction of the electrostatic force  $\vec{F}_{12}$  on particle 1 from particle 2?



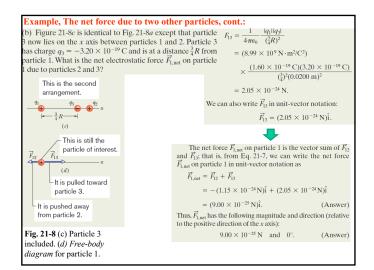


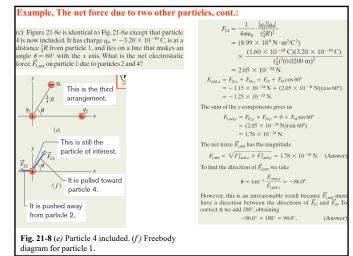


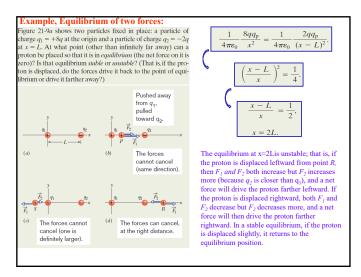
Thus, force  $\vec{F}_{12}$  has the following magnitude and direction (relative to the positive direction of the *x* axis):

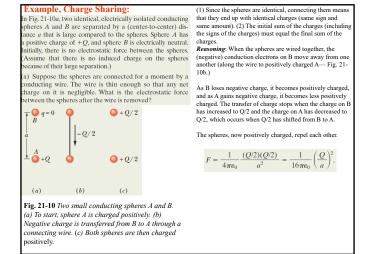
 $1.15\times 10^{-24}\,\rm N\quad and\quad 180^\circ. \tag{Answe}$  We can also write  $\vec{F}_{12}$  in unit-vector notation as

 $\vec{F}_{12} = -(1.15 \times 10^{-24} \,\mathrm{N})\hat{i}$ . (Answer)









#### Example, Charge Sharing, cont.:

(b) Next, suppose sphere A is grounded momentarily, and then the ground connection is removed. What now is the electrostatic force between the spheres?



Fig. 21-10 (d) Negative charge is transferred through a grounding wire to sphere A. (e) Sphere A is then neutral.

**Reasoning:** When we provide a conducting path between a charged object and the ground (which is a huge conductor), we neutralize the object.

Were sphere A negatively charged, the mutual repulsion between the excess electrons would cause them to move from the sphere to the ground.

However, because sphere A is positively charged, electrons with a total charge of Q/2 move from the ground up onto the sphere (Fig. 21-10d), leaving the sphere with a charge of 0 (Fig. 21-10e). Thus, there is (again) no electrostatic force between the two spheres.

#### 21.5 Charge is Quantized

Since the days of Benjamin Franklin, our understanding of of the nature of electricity has changed from being a type of 'continuous fluid' to a collection of smaller charged particles. The total charge was found to always be a multiple of a certain elementary charge, "e":

$$q = ne$$
,  $n = \pm 1, \pm 2, \pm 3, \dots$ 

The value of this elementary charge is one of the fundamental constants of nature, and it is the magnitude of the charge of both the proton and the electron. The value of "e" is:

$$e = 1.602 \times 10^{-19} \,\mathrm{C}.$$

#### 21.5 Charge is Quantized

Table 21-1 The Charges of Three Particles		
Electron	e or e	-e
Proton	p	+e
Neutron	n	0

Elementary particles either carry no charge, or carry a single elementary charge. When a physical quantity such as charge can have only discrete values, rather than any value, we say the quantity is **quantized.** It is possible, For example, to find a particle that has no charge at all, or a charge of +10e, or -6e, but not a particle with a charge of, say, 3.57e.

#### 21.5 Charge is Quantized



Many descriptions of electric charge use terms that might lead you to the conclusion that charge is a substance. Phrases like:

- "Charge on a sphere"
- "Charge transferred"
- "Charge carried on the electron"

However, charge is a *property* of particles, one of many properties, such as mass.

### Example, Mutual Electric Repulsion in a Nucleus:

(a) What is the magnitude of the repulsive electrostatic force between two of the protons that are separated by  $4.0\times10^{-15}~\rm m?$ 

The protons can be treated as charged particles, so the magitude of the electrostatic force on one from the other is iven by Coulomb's law.

Calculation: Table 21-1 tells us that the charge of a proton +e. Thus, Eq. 21-4 gives us

$$\begin{split} F &= \frac{1}{4\pi\epsilon_0} \frac{e^2}{r^2} \\ &= \frac{(8.99 \times 10^8 \, \text{N} \cdot \text{m}^2/\text{C}^2)(1.602 \times 10^{-19} \, \text{C})^2}{(4.0 \times 10^{-15} \, \text{m})^2} \\ &= 14 \, \text{N}. \end{split} \tag{Answer}$$

**No explosion:** This is a small force to be acting on a macroscopic object like a cantaloupe, but an enormous force to be

The nucleus in an iron atom has a radius of about  $4.0 \times 10^{-15}$  m and contains 26 protons.

(a) What is the magnitude of the repulsive electrostatic force between two of the protons that are separated by  $4.0 \times 10^{-15}$  m? electrostatic force.

(b) What is the magnitude of the gravitational force between those same two protons?

#### KEY IDEA

Because the protons are particles, the magnitude of the gravitational force on one from the other is given by Newton's equation for the gravitational force (Eq. 21-2).

**Calculation:** With  $m_{\rm p}$  (= 1.67 × 10<sup>-27</sup> kg) representing the mass of a proton, Eq. 21-2 gives us

$$F = G \frac{m_p^2}{r^2}$$
=  $\frac{(6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2)(1.67 \times 10^{-27} \text{ kg})^2}{(4.0 \times 10^{-15} \text{ m})^2}$   
=  $1.2 \times 10^{-35} \text{ N}$ . (A)

#### 21.6 Charge is Conserved

If one rubs a glass rod with silk, a positive charge appears on the rod. Measurement shows that a negative charge of equal magnitude appears on the silk. This suggests that rubbing does not create charge but only transfers it from one body to another, upsetting the electrical neutrality of each body during the process.

This hypothesis of conservation of charge has stood up under close examination, both for large-scale charged bodies and for atoms, nuclei, and elementary particles.

Example 1: Radioactive decay of nuclei, in which a nucleus transforms into (becomes) a different type of nucleus.

A uranium-238 nucleus (238U) transforms into a thorium-234 nucleus (234Th) by emitting an alpha particle. An alpha particle has the same makeup as a helium-4 nucleus, it has the symbol <sup>4</sup>He. Here the net charge is 238.

$$^{238}U \rightarrow ^{234}Th + ^{4}He$$
,

Example 2: An electron e (charge -e) and its antiparticle, the positron e (charge +e), undergo an annihilation process, transforming into two gamma rays (high-energy light):. Here the net charge is zero.

$$e^- + e^+ {\:\longrightarrow\:} \gamma + \gamma \qquad \text{(annihilation)}.$$

Example 3: A gamma ray transforms into an electron and a positron. Here the net charge is again

$$\gamma \rightarrow e^- + e^+$$
 (pair production).