Chapter 24

Electric Potential

24.1 What is Physics?:

Experimentally, physicists and engineers discovered that the electric force is conservative and thus has an associated electric potential energy.

The motivation for associating a potential energy with a force is that we can then apply the principle of the conservation of mechanical energy to closed systems involving the force.

24.2: Electric Potential Energy

When an electrostatic force acts between two or more charged particles within a system of particles, we can assign an electric potential energy U to the system.

If the system changes its configuration from an initial state i to a different final state f, the electrostatic force does work W on the particles. If the resulting change is ΔU , then $\Delta U = U_f - U_i = -W$.

As with other conservative forces, the work done by the electrostatic force is path independent.

Usually the reference configuration of a system of charged particles is taken to be that in which the particles are all infinitely separated from one another. The corresponding reference potential energy is usually set be zero. Therefore, $U = -W_{\infty}$.

Example, Work and potential energy in an electric field:

Electrons are continually being knocked out of air molecules in (2) The work done by a constant force \vec{F} on a particle under-the atmosphere by cosmic-ray particles coming in from space going a displacement \vec{d} is the atmosphere by cosmic-ray particles coming in from space. Once released, each electron experiences an electrostatic force \overline{F} due to the electric field \overline{E} that is produced in the atmosphere by charged particles already on Earth. Near Earth's surface the elec-The field has the magnitude E = 150 N/C and is directed downward. What is the change ΔU in the electric potential energy of a release electron when the electrostatic force causes it to move vertically upward through a distance d = 520 m (Fig.24-1)?

KEY IDEAS (1) The change ΔU in the electric potential energy of the electron is related to the work W done on the electron by the electric field. Equation 24-1 ($\Delta U = -W$) gives the relation.

$$\vec{E}$$
 \vec{E} \vec{d}

Fig. 24-1 An electron in the atmosphere is moved upward through displacement \vec{d} by an electrostatic force \vec{F} due to an electric field \vec{E} .

 $W = \vec{F} \cdot \vec{d}.$ (24-3) (3) The electrostatic force and the electric field are related by the force equation $\vec{F} = q\vec{E}$, where here q is the charge of an electron (= -1.6×10^{-19} C). **Calculations:** Substituting for \vec{F} in Eq. 24-3 and taking the dot product yield $W = q\vec{E}\cdot\vec{d} = qEd\cos\theta,$ (24-4)

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where \theta is the angle between the directions of \vec{E} and \vec{A}. The field \vec{E} is directed downward and the displacement \vec{d} is directed upward; so \theta = 180^\circ. Substituting this and other data into Eq. 24-4, we find
    W = (-1.6 \times 10^{-19} \text{ C})(150 \text{ N/C})(520 \text{ m}) \cos 180^{\circ}
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= 1.2 \times 10^{-14} \text{ J.}
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Equation 24-1 then yields
  \Delta U = -W = -1.2 \times 10^{-14} \text{ J}.
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(Answer) This result tells us that during the 520 m ascent, the electric potential energy of the electron decreases by $1.2\times10^{-14}\,\rm{J}.$





24.4 Equipotential Surfaces: Adjacent points that have the same electric potential form an equipotential surface, which can be either an imaginary surface or a real, physical surface. No net work W is done on a charged particle by an electric field when the particle moves between two points i and f on the same equipotential surface. Equal work is done along these paths between the same surfaces. No work is done along this path on an equipotential surface Fig. 24-2 Portions of four equipotential surfaces at electric potentials $V_1 = 100 V_2$ $V_2 = 80 V, V_3 = 60 V, and V_4 = 40 V.$ Four paths along which a test charge may move are shown. Two electric field lines are also indicated. No work is done along this path that returns to the same surface







Fig. 24-4 A test charge q_0 moves from point *i* to point *f* along the path shown in a nonuniform electric field. During a displacement $d\vec{s}$, an electrostatic force $q_0\vec{E}$ acts on the test charge. This force points in the direction of the field line at the location of the test charge.



Thus, the potential difference $V_j - V_i$ between any two points i and f in an electric field is equal to the negative of the line integral from i to f. Since the electrostatic force is conservative, all paths yield the same result. If we set potential $V_i = 0$, then

$$V = - \int_{a}^{f} \vec{E} \cdot d\vec{s}$$

 $V = -\int_{i} E \cdot ds,$ This is the potential V at any point f in the electric field relative to the zero potential at point *i*. If point *i* is at infinity, then this is the potential V at any point f relative to the zero potential at infinity.























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Example, Conservation of Mechanical Energy with Electric Potential Energy:

An alpha particle (two protons, two neutrons) moves into a stationary gold atom (79 protons, 118 neutrons), passing through the electron region that surrounds the gold nucleus like a shell and headed directly toward the nucleus (Fig. 24-17). The alpha particle slows until it momentarily stops when its center is at radial distance r = 9.23 fm from the nuclear enter. Then it moves back along its incoming path. (Because the gold nucleus is much more massive than the alpha particle, we can assume the gold nucleus does not move.) What was the kinetic energy K_i of the alpha particle and k atom? Assume that the only force acting between the alpha particle and the gold nucleus is the (electrostatic) Coulomb force.

Fig. 24-17 An alpha particle, traveling head-on toward the center of a gold nucleus, comes to a momentary stop (at which time all its kinetic energy has been transferred to electric potential energy) and then reverses its path.

Reasoning: When the alpha particle is outside the atom, he system's initial electric potential energy U, is zero beause the atom has an equal number of electrons and proons, which produce a *net* electric field of zero. However, once the alpha particle passes through the electron region aurrounding the nucleus on its way to the nucleus, the elecric field due to the electrons goes to zero. The reason is that

Alpha particle

Gold nucleus

the electrons act like a closed spherical shell of uniform ne
ative charge and, as discussed in Section 23-9, such a she
produces zero electric field in the space it encloses. The a
pha particle still experiences the electric field of the protor
in the nucleus, which produces a repulsive force on the pro-
tons within the alpha particle.
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As the incoming alpha particle is slowed by this repulsiv force, its kinetic energy is transferred to electric potentic energy of the system. The transfer is complete when the alph particle momentarily stops and the kinetic energy is $K_f = 0$. **Calculations:** The principle of conservation of mechanical

ergy tells us that		
	$K_i + U_i = K_\ell + U_\ell$	(24-

We know two values: $U_i = 0$ and $K_f = 0$. We also know that the potential energy U_j at the stopping point is given by the right side of Eq. 24-43, with $q_1 = 2e, q_2 = 79e$ (in which *e* is the elementary charge. 1.60×10^{-19} C), and r = 9.23 fm Thus, we can rewrite Eq. 24-44 as

$K_i =$	$\frac{1}{4\pi\epsilon_0} \frac{(2e)(79e)}{9.23 \text{ fm}}$
=	$\frac{(8.99 \times 10^9 \mathrm{N} \cdot \mathrm{m^2/C^2})(158)(1.60 \times 10)}{9.23 \times 10^{-15} \mathrm{m}}$
=	$3.94 \times 10^{-12} \text{ J} = 24.6 \text{ MeV}.$

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24.12 Potential of a Charges, Isolated Conductor:				
An excess charge placed on an isolated conductor will distribute itself on the surface of that conductors that all points of the conductor — whether on the surface or inside — come to the same potential. This is true even if the conductor has an internal cavity and even if that cavity contains a net charge.				
We know that $V_f - V_i = -\int_i^f \vec{E} \cdot d\vec{x}$				
Since for all points $E = 0$ within a conductor, it follows directly that $V_f = V_i$ for all possible pairs of points <i>i</i> and <i>f</i> in the conductor.				
$\mathbf{Fig. 24-18} (a) \text{ A plot of } V(r) both inside and outside a charged spherical shell of radius 10 m (b) A plot of E(r) for the same shell.$				

24.12 Spark Discharge from a Charge Conductor:

Fig. 24-19 A large spark jumps to a car's body and then exits by moving across the insulating left front tire (note the flash there), leaving the person inside unharmed. (Courtesy Westinghouse Electric Corporation)



On nonspherical conductors, a surface charge does not distribute itself uniformly over the surface of the conductor. At sharp points or edges, the surface charge density—and thus the external electric field, —may reach very high values. The air around such sharp points or edges may become ionized, producing the corona discharge that golfers and mountaineers see on the tips of bushes, golf clubs, and rock hammers when thunderstorms threaten. Such corona discharges are often the precursors of lightning strikes. In such circumstances, it is wise to enclose yourself in a cavity inside a conducting shell, where the electric field is guaranteed to be zero. A car (unless it is a convertible or made with a plastic body) is almost ideal

24.12 Isolated Conductor in an Isolated Electric Field:



Fig. 24-20 An uncharged conductor is suspended in an external electric field. The free electrons in the conductor distribute themselves on the surface as shown, so as to reduce the net electric field inside the conductor to zero and make the net field at the surface perpendicular to the surface. If an isolated conductor is placed in an external electric field, all points of the conductor still come to a single potential regardless of whether the conductor has an excess charge.

The free conduction electrons distribute themselves on the surface in such a way that the electric field they produce at interior points cancels the external electric field that would otherwise be there.

Furthermore, the electron distribution causes the net electric field at all points on the surface to be perpendicular to the surface. If the conductor in Fig. 24-20 could be somehow removed, leaving the surface charges frozen in place, the internal and external electric field would remain absolutely unchanged.