

Review for Celebration #2

Review for Test #2

Chapter 26: Current & Resistance

current $i = \frac{dq}{dt}$ units of $i \rightarrow$ amp (A) $1 \text{ A} = 1 \text{ C/s}$

conventional current \Rightarrow flow of hypothetical + charge from + to - terminal of battery

\downarrow in reality, electrons flow in opposite direction

$i = \int \vec{J} \cdot d\vec{A}$ \rightarrow always applies
current density $\vec{J} = i/A$ $[J] = \text{A/m}^2$

drift speed $V_d = \frac{i}{nAe}$

\downarrow applies if i is uniform and parallel to $d\vec{A}$

$V_d = J/ne \rightarrow \vec{J} = (ne)\vec{V}_d$

definition of resistance

$$R = V/i$$

units of $R \rightarrow$ ohm (Ω)

$$1 \Omega = 1 \text{ V/A}$$

resistivity $\rho = E/J$

units of $\rho \rightarrow \Omega \text{ m}$

$$\vec{E} = \rho \vec{J}$$

conductivity $\sigma = 1/\rho$ \rightarrow units of $(\Omega m)^{-1}$

$$\vec{J} = 1/\rho \vec{E} = \sigma \vec{E}$$

resistance of a conducting wire $\Rightarrow R = \rho L/A$

$$\rho - \rho_0 = \rho_0 \alpha (T - T_0)$$
$$R - R_0 = R_0 \alpha (T - T_0)$$

$\alpha \rightarrow$ temp. coeff. of resistivity
 \downarrow
units of α are $(K)^{-1}$ or $(C^\circ)^{-1}$

"Ohm's Law" $\rightarrow V = iR \quad i = V/R \quad R = V/i$

\downarrow
a conductor obeys Ohm's law if R is a constant independent of magnitude & polarity of voltage

$P = iV$ \rightarrow holds true for any electrical device

$P = i^2 R$
 $P = V^2/R$ \rightarrow only holds true for resistors

Chapter 27: Circuits

emf $\mathcal{E} \rightarrow$ defined as $\mathcal{E} = dW/dq$

voltage across a battery with internal resistance r is given by:

$$V = \mathcal{E} - i r$$

for n resistors in series:

$$R_{eq} = \sum_{i=1}^n R_i$$

for n resistors in parallel:

$$\frac{1}{R_{eq}} = \sum_{i=1}^n \frac{1}{R_i}$$

* resistors in series have same i as R_{eq}

* resistors in parallel have same V as R_{eq}

Kirchoff's junction rule $\Rightarrow i_{in} = i_{out}$

Kirchoff's loop rule $\Rightarrow \sum V = 0$ around any closed loop



algebraic sum of the changes in potential around any closed loop is zero

sign conventions for Kirchhoff's loop rule:

emf devices → going through emf device from - to + terminal,
the change in potential is $+E$

↓
from + to - terminal, change in potential is $-E$

resistor → going through resistor in same direction as current,
the change in potential is $-iR$

↓
in opposite direction as current, the change in
potential is $+iR$

* if you do not know the direction of the current,
assume a direction → if i comes out negative, your
assumed direction was wrong

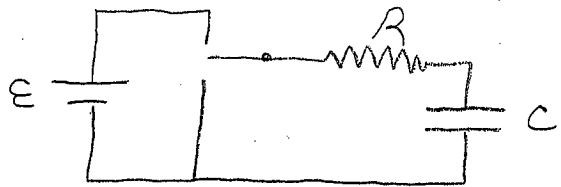
⇒ for an emf device $P = iE$

* know how to calculate the potential difference between
2 points or the potential at one point given the potential
at another point

ammeter → very small R (connected in series)

voltmeter → very large R (connected in parallel)

RC Circuits



charging a capacitor:

$$q = q_0 (1 - e^{-t/\tau}) = C\mathcal{E} (1 - e^{-t/\tau})$$

$$V = q/C = \mathcal{E} (1 - e^{-t/\tau})$$

$$i = dq/dt = \mathcal{E}/R e^{-t/\tau}$$

$$\tau = RC$$

↓
capacitive time
constant

discharging a capacitor:

$$q = q_0 e^{-t/\tau}$$

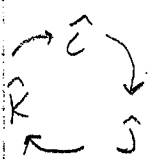
$$i = dq/dt = - (q_0/RC) e^{-t/\tau}$$

Chapter 28: Magnetic Fields

$$\boxed{\vec{F}_B = q \vec{v} \times \vec{B}} \rightarrow \text{magnitude of } F_B = q v B \sin \theta$$

↓

direction given by RHR \Rightarrow curl fingers of right hand from \vec{v} into \vec{B} , thumb points in direction of \vec{F} on a positive charge (opposite direction if charge is negative)



$$\begin{aligned} \hat{i} \times \hat{j} &= \hat{k} \\ \hat{j} \times \hat{k} &= \hat{i} \\ \hat{k} \times \hat{i} &= \hat{j} \end{aligned}$$

$$\begin{aligned} \hat{j} \times \hat{i} &= -\hat{k} \\ \hat{k} \times \hat{j} &= -\hat{i} \\ \hat{i} \times \hat{k} &= -\hat{j} \end{aligned}$$

Joe's RHR \Rightarrow

thumb $\rightarrow \vec{v}$
 fingers $\rightarrow \vec{B}$
 palm $\rightarrow \vec{F}$

$$\vec{v} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ v_x & v_y & v_z \\ B_x & B_y & B_z \end{vmatrix} = \hat{i} \begin{vmatrix} v_y & v_z \\ B_y & B_z \end{vmatrix} - \hat{j} \begin{vmatrix} v_x & v_z \\ B_x & B_z \end{vmatrix} + \hat{k} \begin{vmatrix} v_x & v_y \\ B_x & B_y \end{vmatrix}$$

* \vec{F}_B is always \perp to both \vec{v} and \vec{B}

↓

magnetic fields can not change the speed of a moving charged particle, only the direction of the particle

unit of $\vec{B} \rightarrow$ tesla (T)

$$\boxed{1 \text{ T} = 1 \text{ N/A}\cdot\text{m}}$$

\Rightarrow if both \vec{E} + \vec{B} fields are present :

$$\boxed{\vec{F} = q (\vec{E} + \vec{v} \times \vec{B})}$$

⇒ for crossed $\vec{E} + \vec{B}$ fields in opposition, the net force on a charged particle is zero if:

$$v = E/B$$

Circulating Charged Particle

$$r = \frac{mv}{qB}$$

$$T = \frac{2\pi m}{qB}$$

$$f = \frac{qB}{2\pi m}$$

↓
above equations apply if $\vec{v} \perp \vec{B}$

⇒ if \vec{v} is not \perp to \vec{B} , the particle moves in a helical path

radius of helix

$$r = \frac{m v_{\perp}}{qB}$$

$$v_{\perp} = v \sin \theta$$

pitch

$$p = v_{\parallel} T$$

$$v_{\parallel} = v \cos \theta$$

magnetic force on a current-carrying wire

$$\vec{F} = i \vec{L} \times \vec{B}$$

↓
magnitude of $F = i L B \sin \theta$

direction of \vec{F} from RHR ⇒ curl fingers of RH from \vec{L} (which is in direction of conventional current) into \vec{B} , thumb points in direction of \vec{F}

⇒ the net force on a closed current-carrying loop of wire in a uniform \vec{B} -field is zero

↓ however, current loop may experience a torque

$$\tau = N i A B \sin \theta$$

magnetic dipole moment

$$\mu = N i A$$

↓
direction of $\vec{\mu}$ ⇒ curl fingers of RH in direction of conventional current, thumb points in direction of $\vec{\mu}$

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

⇒ potential energy of a magnetic dipole in an external magnetic field is given by:

$$U = -\vec{\mu} \cdot \vec{B}$$

Chapter 29: Magnetic Fields Due to Currents

Biot-Savart law \Rightarrow

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{i d\vec{s} \times \vec{r}}{r^3}$$



magnitude

$$dB = \frac{\mu_0}{4\pi} \frac{i ds \sin\theta}{r^2}$$



direction of $d\vec{B}$ is given by $d\vec{s} \times \vec{r}$

$$\vec{B} = \int d\vec{B}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ Tm/A} \approx 1.26 \times 10^{-6} \text{ Tm/A}$$

long (infinite) straight wire \Rightarrow

$$B = \frac{\mu_0 i}{2\pi r}$$

semi-infinite straight wire \Rightarrow

$$B = \frac{\mu_0 i}{4\pi r}$$

center of circular arc of radius R
and angle ϕ (in radians) \Rightarrow

$$B = \frac{\mu_0 i \phi}{4\pi R}$$

force between two parallel currents \Rightarrow

$$F = \frac{\mu_0 L i_1 i_2}{2\pi d}$$

* parallel currents attract, antiparallel currents repel

Ampere's law \Rightarrow

$$\oint \vec{B} \cdot d\vec{S} = \mu_0 i_{\text{encl}}$$

RHR for Ampere's law \Rightarrow curl fingers of RH in direction of Amperian loop; currents in general direction of thumb are +, currents in opposite direction are -

inside long straight wire with uniform current density \Rightarrow

$$B = \left(\frac{\mu_0 i}{2\pi R^2} \right) r$$

ideal solenoid \Rightarrow

$$B = \mu_0 i n$$

$n = \# \text{ turns per unit length}$



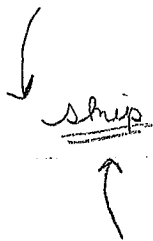
B inside solenoid

B = 0 outside ideal solenoid

inside toroid

$$B = \frac{\mu_0 i N}{2\pi r}$$

B = 0 outside toroid



$$\vec{B}(z) = \frac{\mu_0}{2\pi} \frac{\vec{\mu}}{z^3}$$

\rightarrow \vec{B} a distance z above center of a current carrying coil

$$\mu = N i A$$