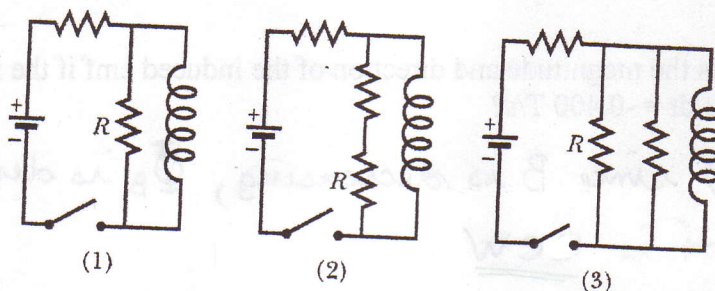


### Quiz #8: Induction and Inductance

#### Problem 1 (2 points)

The figure below shows three circuits with identical batteries, inductors, and resistors. In each circuit, the switch has been closed for a *very long time*. Rank the circuits according to the current through the resistor labeled R (a) immediately after the switch is reopened, and (b) a long time after the switch is reopened, greatest first.

- 1) (a)  $1 > 2 > 3$  (b) all tie  
2) (a)  $1 = 3 > 2$  (b) all tie  
3) (a)  $1 = 2 > 3$  (b) all tie  
4) (a)  $1 > 2 > 3$  (b)  $1 = 3, 2$   
5) none of the above

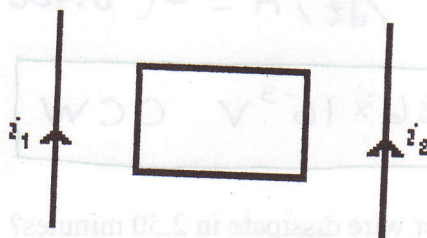


#### Problem 2 (2 points)

A rectangular loop of wire is placed midway between two long straight parallel wires as shown. The wires carry currents  $i_1$  and  $i_2$  as indicated. What is the direction of the induced current (if any) in the rectangular loop if (a)  $i_1$  is increasing and  $i_2$  is constant, (b) both  $i_1$  and  $i_2$  are decreasing at the same rate?

a) CCW

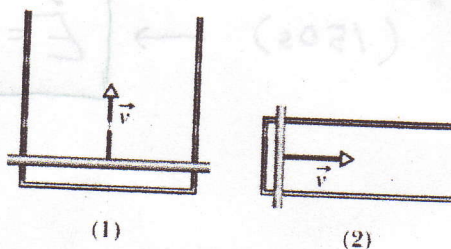
b) no induced current



↓ flux through loop is zero

#### Problem 3 (2 points)

The figure below shows two circuits in which a conducting bar is slid at the same speed  $v$  through the same uniform magnetic field and along a U-shaped wire. The parallel lengths of the wire are separated by  $2L$  in circuit 1 and by  $L$  in circuit 2. The current induced in circuit 1 is clockwise. (a) Is the direction of the magnetic field into or out of the page? (b) Is the emf induced in circuit 1 larger than, smaller than, or the same as that in circuit 2?



a) out of page

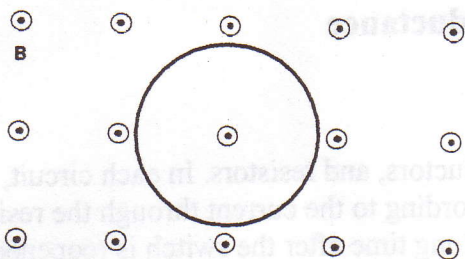
b) larger than

↓  $\Phi_B$  is changed more because area is changing more



**Problem 4 (4 points)**

A copper wire with resistance  $R = 2.50 \Omega$  and length  $32.5 \text{ cm}$  is formed into a circular loop and placed in a uniform magnetic field pointing out of the page as shown below.



$$C = 2\pi r = 0.325 \text{ m}$$

$$r = 0.0517 \text{ m}$$

- a) What is the magnitude and direction of the induced emf if the magnitude of the magnetic field decreases at a rate of  $dB/dt = -0.400 \text{ T/s}$ ?

$\Rightarrow$  since  $B$  is decreasing,  $\Phi_B$  is decreasing so the induced emf is CCW

$$\mathcal{E} = -N d\Phi_B/dt \quad N=1 \quad \Phi_B = BA \quad A = \pi r^2$$

$$\mathcal{E} = -d/dt (BA) = -(dB/dt) A = -(-0.400 \text{ T/s}) \pi (0.0517 \text{ m})^2$$

$$\mathcal{E} = 3.36 \times 10^{-3} \text{ V CCW}$$

- b) How much energy will the copper wire dissipate in 2.50 minutes?

$$P = \mathcal{E}/t \rightarrow \mathcal{E} = Pt \quad P = \mathcal{E}^2/R \text{ for resistor}$$

$$\mathcal{E} = (\mathcal{E}^2/R) t$$

$$\mathcal{E} = \frac{(3.36 \times 10^{-3} \text{ V})^2}{2.50 \Omega} (150 \text{ s}) \rightarrow \mathcal{E} = 6.73 \times 10^{-4} \text{ J}$$