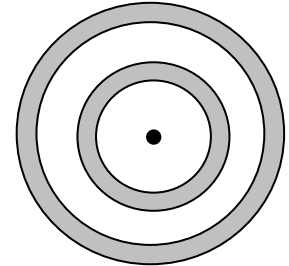


## Celebration #1: Chapters 21 – 25

### Short Answer Questions (5 or 6 points each)

#### Question 1 (6 points)

A  $+20\mu\text{C}$  point charge is surrounded by 2 conducting spherical shells as shown in the figure to the right. The inner shell has a charge of  $+15\mu\text{C}$  and has an inner radius  $R_a$  and outer radius  $R_b$ . The outer shell has a charge of  $-10\mu\text{C}$  and has an inner radius  $R_c$  and outer radius  $R_d$



What is the charge on the **inner** surface of the **inner** shell (at radius  $R_a$ )?

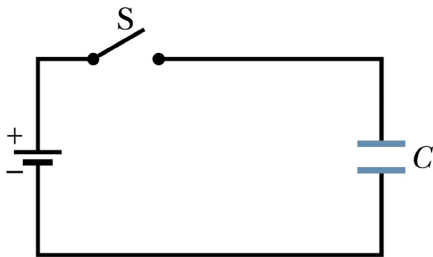
What is the charge on the **outer** surface of the **inner** shell (at radius  $R_b$ )?

What is the charge on the **inner** surface of the **outer** shell (at radius  $R_c$ )?

What is the charge on the **outer** surface of the **outer** shell (at radius  $R_d$ )?

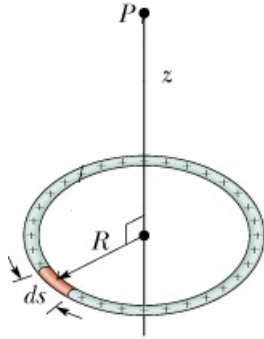
#### Question 2 (6 points)

The capacitor in the figure below has a capacitance of  $25.0\mu\text{F}$  and is initially uncharged. The battery provides a potential difference is  $15.0\text{V}$ . After the switch is closed, how many electrons will flow from the battery to the bottom plate of the capacitor?



**Question 3** (5 points)

The electric potential at point P, a distance  $z$  from central axis of a thin ring of radius  $R$  and linear charge density  $\lambda$ , can be written as  $V = \lambda R / (2\epsilon_0 \sqrt{z^2 + R^2})$ . Show that both sides of this equation have the same units.

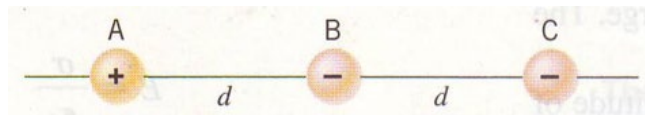


**Question 4** (5 points)

You are given the potential function  $V(x,y) = 6xy^3 + 3x^2y$ , where  $V$  is in volts and  $x$  and  $y$  are in meters. Determine the magnitude of the electric field  $\mathbf{E}$  at the point  $x = 1, y = 2$ .

**Question 5** (6 points)

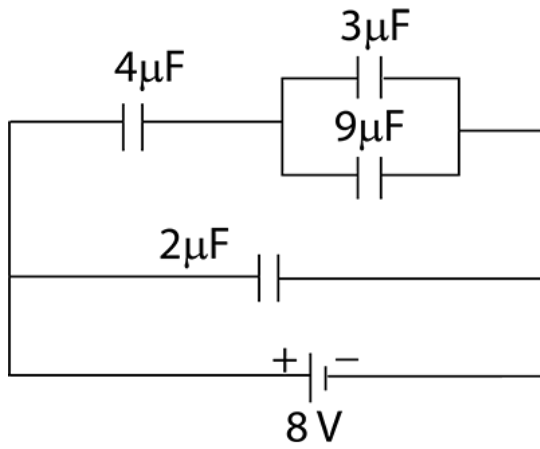
Three point charges have equal magnitudes. They are fixed in place on the same straight line, and are equally separated by a distance  $d$ . Consider the net electrostatic force acting on each charge. Calculate the ratio of the largest to the smallest net force.



## Problems (12 points each)

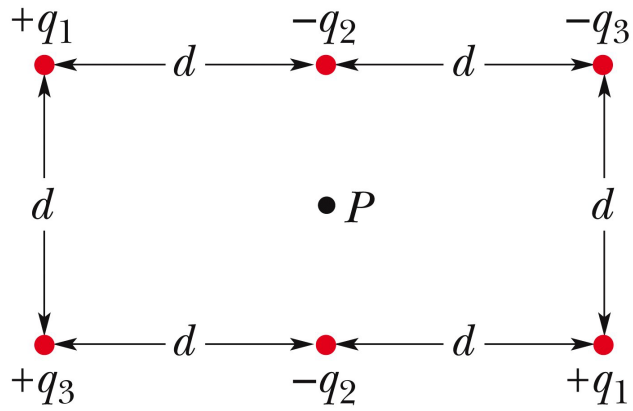
### Problem 1

In the circuit shown below, what is the charge on and the potential difference across each capacitor?



### Problem 2

In the figure below, point P is at the center of the rectangle,  $q_1 = 4.00 \text{ pC}$ ,  $q_2 = 2.50 \text{ pC}$ ,  $q_3 = 5.00 \text{ pC}$ , and  $d = 3.50 \text{ cm}$ . (a) What is the net electric potential at point P due to the six charged particles? (b) What is the magnitude and direction of the net electric field at point P due to the six charged particles?



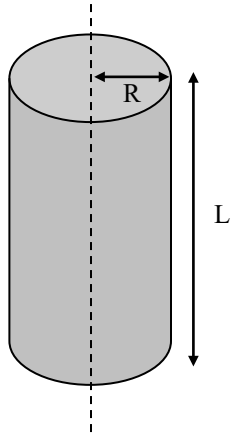
Copyright © 2011 John Wiley & Sons, Inc. All rights reserved.

halliday\_9e\_fig\_24\_65

### Problem 3

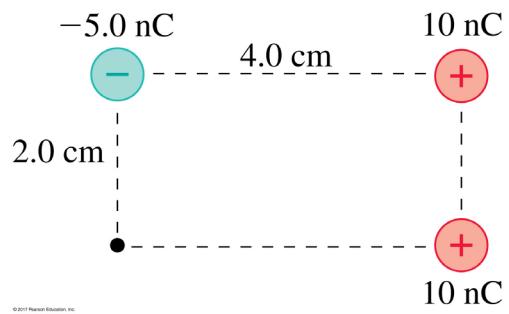
A long, solid *nonconducting* cylinder of length  $L$  and radius  $R$  has a nonuniform charge distribution of volume charge density  $\rho = Ar/R$ , where  $r$  is the radial distance from the cylindrical axis and  $A$  is a constant. Using Gauss' law, derive an expression for the electric field a radial distance  $r$  from the axis of the cylinder for points **(a)** inside the cylinder ( $r < R$ ), and **(b)** outside the cylinder ( $r > R$ ).

**Hint:**  $q = \int \rho dV = \int \rho(2\pi rL)dr$



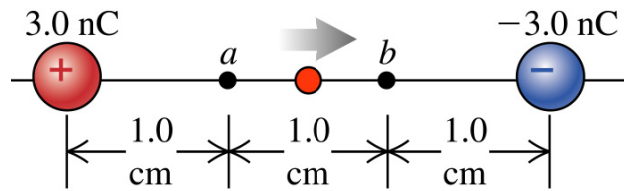
**Problem 4**

What is the magnitude and direction of the net electrostatic force on the  $-5.0\text{ nC}$  charge?



**Problem 5**

A dust particle with mass  $5.0 \mu\text{g}$  and charge  $2.0 \text{ nC}$  starts from rest at point  $a$  and moves in a straight line to point  $b$ . What is its speed at point  $b$ ?



**Problem 6**

Charge  $Q = 30.0 \text{ nC}$  is uniformly distributed along a thin, flexible rod of length  $L = 15.0 \text{ cm}$ . The rod is bent into a semicircle as shown in the figure below. What is the magnitude and direction of the electric field at the center of the semicircle?

